# Inductive Proof Outlines for Monitors in Java\*

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**Abstract.** The research concerning Java's semantics and proof theory has mainly focussed on various aspects of sequential sub-languages. Java, however, integrates features of a class-based object-oriented language with the notion of multi-threading, where multiple threads can concurrently execute and exchange information via shared instance variables. Furthermore, each object can act as a monitor to assure mutual exclusion or to coordinate between threads.

In this paper we present a sound and relatively complete assertional proof system for Java's monitor concept, which generates verification conditions for a concurrent sublanguage  $Java_{MT}$  of Java. This work extends previous results by incorporating Java's monitor methods.

**Keywords:** OO, Java, multithreading, monitors, deductive verification, proof-outlines

# 1 Introduction

From its inception, Java [12] has attracted interest from the formal methods community: The widespread use of Java across platforms made the need for formal studies and verification support more urgent, the grown awareness and advances of formal methods for real-life languages made it more acceptable, and last but not least the array of non-trivial language features made it challenging.

Nevertheless, research concerning Java's proof theory concentrated mainly on various aspects of *sequential* sub-languages (see e.g. [14, 23, 20]). In [5], we presented a sound and complete proof method for multithreaded Java, where threads can concurrently execute and exchange information via shared instance variables. In this paper we extend our results to deal with Java's monitor synchronization mechanism: each object can act as a monitor to assure mutual exclusion or to coordinate between threads.

To support a clean interface between internal and external object behavior, we exclude qualified references to instance variables. As a consequence, sharedvariable concurrency is caused by simultaneous execution within a single object, only, but not across object boundaries. In order to capture program behavior

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in a modular way, the assertional logic and the proof system are formulated in two levels, a local and a global one. The local assertion language describes the internal object behavior. The global behavior, including the communication topology of the objects, is expressed in the global language. As in the Object Constraint Language (OCL) [24], properties of object-structures are described in terms of a navigation or dereferencing operator.

The assertional proof system for safety properties is formulated in terms of *proof outlines* [19], i.e., of programs augmented by auxiliary variables and annotated with Hoare-style assertions [11, 13]. Invariance of the asserted program properties is guaranteed by the verification conditions of the proof system. The execution of a single method body in isolation is captured by standard *local correctness* conditions, using the local assertion language. Interference between concurrent method executions is covered by the *interference freedom test* [19, 16], formulated also in the local language. It has especially to accommodate for reentrant code and the specific synchronization mechanism. Possibly affecting more than one instance, communication and object creation are treated in the *cooperation test*, using the global language. The theory presented here forms the theoretical foundation for a verification tool (Verger) which takes asserted Java programs as input and generates verification conditions for the PVS theorem prover as output; the use of the tool on a number of examples is reported in [4].

**Overview** The paper is organized as follows. Section 2 defines syntax and semantics of the programming language. After introducing the assertional logic in Section 3, the main Section 4 presents the proof system. Section 5 discusses related and future work.

# 2 The programming language Java<sub>MT</sub>

Similar to Java, the language  $Java_{MT}$  is strongly typed; besides class types c, it supports booleans and integers as primitive types, and products and lists as composite types. Each corresponding value domain is equipped with a standard set of operators with typical element f; we use  $\alpha, \beta, \ldots$  as typical object identities.

# 2.1 Syntax

The  $Java_{MT}$  syntax is summarized in Table 1. We notationally distinguish between *instance* variables  $x \in IVar$ , and stack-allocated *local* or *temporary* variables  $u \in TVar$  of methods; we use y to denote variables from  $Var = IVar \cup$ TVar. Programs are collections of classes containing method declarations, where we use c and m for class names resp. method names, and  $body_{m,c}$  to refer to the body of method m in class c. *Instances* of the classes, i.e., *objects*, are dynamically created, and communicate via *method invocation*. To increase readability of the proof outlines, we deviate from standard *Java* syntax, in that method invocation is syntactically split into a sending and a receiving statement.

```
exp ::= x \mid u \mid this \mid nil \mid f(exp, ..., exp)
      exp_{ret} ::= \epsilon \mid exp
         u_{ret} ::= \epsilon \mid u
         stm ::= \epsilon \mid x := exp \mid u := exp \mid u := \mathsf{new}^c \mid exp.m(exp, \ldots, exp); receive u_{ret}
                 | exp.start() | stm; stm | if exp then stm else stm fi | while exp do stm od ...
      modif ::= nsync | sync
       meth ::= modifm(u, \ldots, u) \{ stm; return exp_{ret} \}
    meth_{run} ::= modifrun() \{ stm; return \}
   meth_{start} ::= nsync start() \{ this.run(); receive; return \}
   meth_{wait} ::= nsyncwait() \{ ?signal; return_{getlock} \}
  meth_{notify} ::= nsync notify() \{ !signal ; return \}
meth_{notifyAll} ::= nsync notifyAll() \{ !signal_all; return \}
   meth_{main} ::= nsync main() \{ stm; return \}
        class ::= c\{meth...meth meth_{run} meth_{start} meth_{wait} meth_{notify} meth_{notifyAll}\}
   class_{main} ::= c\{meth...meth\ meth_{run}\ meth_{start}\ meth_{wait}\ meth_{notify}\ meth_{notifyAll}\ meth_{main}\}
        prog ::= \langle class \dots class \ class_{main} \rangle
```

Table 1.  $Java_{MT}$  abstract syntax

Each class contains the predefined methods start, wait, notify, and notifyAll, and furthermore a user-defined run-method. The entry point of the program is given by the main-method of the program's main class. Invocation of the start-method, which can be done successfully only once, spawns a new thread of execution while the initiating thread continues its own execution.

As a mechanism of concurrency control, methods can be declared as *synchronized*. Each object has a *lock* which can be owned by at most one thread. Synchronized methods of an object can be invoked only by a thread that owns the lock of that object. Without the lock, a thread has to wait until the lock becomes free. The owner of an object's lock can recursively invoke several synchronized methods of that object, which corresponds to the notion of reentrant monitors. The monitor methods wait, notify, and notifyAll facilitate efficient thread coordination at the object boundary. Their definitions use the auxiliary statements lsignal, lsignal\_all, ?signal, and return<sub>getlock</sub>. A thread owning the lock of an object can block itself and free the lock by invoking wait on the object. The blocked thread can be reactivated by another thread via the object's notify-method; the reactivated thread must re-apply for the lock before it may continue its execution. The method notifyAll, finally, notifies all threads blocked on the object.

#### 2.2 Operational semantics

A local state  $\tau$  holds the values of the local variables of a method. A local configuration  $(\alpha, \tau, stm)$  of a thread executing within an object  $\alpha \neq nil$  specifies, in addition to its local state  $\tau$ , its point of execution represented by the statement stm. A thread configuration  $\xi = (\alpha_0, \tau_0, stm_0) \dots (\alpha_n, \tau_n, stm_n)$  is a stack of local

$m \in \{\text{wait, notify, notifyAll}\}$ $\beta = \llbracket e \rrbracket_{\mathcal{E}}^{\sigma(\alpha), \tau} \in dom(\sigma) \qquad owns(\xi \circ (\alpha, \tau, e.m(); stm), \beta)$ $(T \vdash \{\xi \circ (\alpha, \tau, e.m(); stm)\}, \sigma) \longrightarrow (T \vdash \{\xi \circ (\alpha, \tau, e.m) \circ (\beta, \tau^{m,c}, hody, \dots)\}, \sigma)$	$CALL_{monitor}$	
$(1 \cup \{\zeta \cup (\alpha, \gamma, e.m(), sem)\}, o) \longrightarrow (1 \cup \{\zeta \cup (\alpha, \gamma, sem) \cup (\beta, \gamma_{init}, observation)\}, o)$		
$\neg owns(T, \beta)$	– Return <sub>wait</sub>	
$\langle T \mathrel{\dot{\cup}} \{ \xi \circ (\alpha, \tau, receive; stm) \circ (\beta, \tau', return_{getlock}) \}, \sigma \rangle \longrightarrow \langle T \mathrel{\dot{\cup}} \{ \xi \circ (\alpha, \tau, stm) \}, \sigma \rangle$		
$ \frac{\langle T \ \dot{\cup} \ \{\xi \circ (\alpha, \tau, \texttt{lsignal}; stm)\} \ \dot{\cup} \ \{\xi' \circ (\alpha, \tau', \texttt{lsignal}; stm')\}, \sigma \rangle \longrightarrow}{\langle T \ \dot{\cup} \ \{\xi \circ (\alpha, \tau, stm)\} \ \dot{\cup} \ \{\xi' \circ (\alpha, \tau', stm')\}, \sigma \rangle} $		
$wait(T, \alpha) = \emptyset$		
$\langle T \stackrel{\cdot}{\cup} \{\xi \circ (\alpha, \tau, ! \text{signal}; stm)\}, \sigma \rangle \longrightarrow \langle T \stackrel{\cdot}{\cup} \{\xi \circ (\alpha, \tau, stm)\}, \sigma \rangle$		
$T' = signal(T, \alpha)$		
$\langle T \stackrel{\cdot}{\cup} \{ \xi \circ (\alpha, \tau, ! \text{signal\_all}; stm) \}, \sigma \rangle \longrightarrow \langle T' \stackrel{\cdot}{\cup} \{ \xi \circ (\alpha, \tau, stm) \}, \sigma \rangle$		

Table 2. Operational semantics of the monitor methods

configurations, representing the call chain of the thread. We write  $\xi \circ (\alpha, \tau, stm)$  for pushing a new local configuration onto the stack.

An object is characterized by its *instance state*  $\sigma_{inst}$  which assigns values to the self-reference this and to instance variables. The initial states  $\tau_{init}$  and  $\sigma_{inst}^{init}$  assign initial values to all variables. A global state or heap  $\sigma$  maps each currently existing object, i.e., an object of its domain, to its instance state. A global configuration  $\langle T, \sigma \rangle$  consists of a set T of thread configurations of the currently executing threads, together with a global state  $\sigma$ .

Expressions are evaluated with respect to an *instance local* state  $(\sigma_{inst}, \tau)$ ; the base cases are  $\llbracket u \rrbracket_{\mathcal{E}}^{\sigma_{inst},\tau} = \tau(u), \llbracket x \rrbracket_{\mathcal{E}}^{\sigma_{inst},\tau} = \sigma_{inst}(x)$ , and  $\llbracket \text{this} \rrbracket_{\mathcal{E}}^{\sigma_{inst},\tau} = \sigma_{inst}(\text{this})$ . The operational semantics is given as transitions between global configurations. A program's initial configuration  $\langle T_0, \sigma_0 \rangle$  satisfies  $T_0 = \{(\alpha, \tau_{init}, body_{\min,c})\}$  and  $\sigma_0(\alpha) = \sigma_{inst}^{init}[\text{this} \mapsto \alpha]$ , where the domain of  $\sigma_0$  is  $\{\alpha\}$  and  $\alpha$  is an instance of the main class c.

For the semantics of assignment, object and thread creation, and ordinary method invocation we refer to [4]. The rules of Table 2 handle  $Java_{MT}$ 's monitor methods wait, notify, and notifyAll, offering a typical monitor synchronization mechanism. In all three cases the caller must own the lock of the callee object (cf. rule CALL<sub>monitor</sub>), as expressed by the predicate *owns*, defined below.

A thread can *block* itself on an object whose lock it owns by invoking the object's wait-method, thereby relinquishing the lock and placing itself into the object's wait set. Formally, the wait set  $wait(T, \alpha)$  of an object is given as the set

of all stacks in T with a top element of the form  $(\alpha, \tau, ?signal; stm)$ . After having "put itself on ice", the thread awaits notification by another thread which invokes the notify-method of the object. The !signal-statement in the notify-method thus reactivates a single thread waiting for notification on the given object (cf. rule SIGNAL). Analogous to the wait set, the notified set  $notified(T, \alpha)$  of  $\alpha$  is the set of all stacks in T with top element of the form  $(\alpha, \tau, return_{getlock})$ , i.e., threads which have been notified and trying to get hold of the lock again. According to rule RETURN<sub>wait</sub>, the receiver can continue after notification in executing return<sub>getlock</sub> only if the lock is free. Note that the notifier does not hand over the lock to the one being notified but continues to own it. This behavior is known as *signal-and-continue* monitor discipline [6].

If no threads are waiting on the object, the !signal of the notifier is without effect (cf. rule SIGNAL<sub>skip</sub>). The notifyAll-method generalizes notify in that all waiting threads are notified via the !signal\_all-broadcast (cf. rule SIGNALALL). The effect of this statement is given by setting  $signal(T, \alpha)$  as  $(T \setminus wait(T, \alpha)) \cup \{\xi \circ (\beta, \tau, stm) \mid \xi \circ (\beta, \tau, ?signal; stm) \in wait(T, \alpha)\}.$ 

Using the wait and notified sets, we can now formalize the *owns* predicate: A thread  $\xi$  owns the lock of  $\beta$  iff  $\xi$  executes some synchronized method of  $\beta$ , but not its wait-method. Formally,  $owns(T, \beta)$  is true iff there exists a thread  $\xi \in T$ and a  $(\beta, \tau, stm) \in \xi$  with stm synchronized and  $\xi \notin wait(T, \beta) \cup notified(T, \beta)$ . An invariant of the semantics is that at most one thread can own the lock of an object at a time.

# 3 The assertion language

Java<sub>MT</sub> does not allow qualified references to instance variables, to support a clean interface between between internal and external object behavior. To mirror this modularity, the assertion logic consists of a *local* and a *global* sublanguage. Local assertions are used to annotate methods in terms of their local variables and of the instance variables of the class to which they belong. Global assertions describe a whole system of objects and their communication structure and will be used in the cooperation test. In the assertion language we add the type **Object** as the supertype of all classes, and we introduce *logical variables*  $z \in LVar$  different from all program variables. Logical variables are used for quantification and as free variables to represent local variables in the global assertion language. Expressions and assertions are interpreted relative to a logical environment  $\omega$ , assigning values to logical variables.

Assertions are built using the usual constructs from predicate logic (cf. Table 3), where only the difference between the local and the global level deserves mention which concerns the form of quantification. On the local language, unrestricted quantification  $\exists z.p$  is solely allowed for integer and boolean domains, but not for reference types, as for those types the range of quantification dynamically depends on the *global* state, something one cannot speak about on the local level. Nevertheless, one can assert the existence of objects on the local level, provided one is explicit about the domain of quantification, as in the

$exp_l ::= z \mid x \mid u \mid this \mid null \mid f(exp_l, \dots, exp_l)$	$e \in LExp$
$\begin{array}{l} ass_l ::= exp_l \mid \neg ass_l \mid ass_l \land ass_l \\ \mid \exists z. \; ass_l \mid \exists z \in exp_l. \; ass_l \mid \exists z \sqsubseteq exp_l. \end{array}$	$ass_l \ p \in LAss$
$exp ::= z \mid null \mid f(exp \ldots exp) \mid exp x$	$E \in GExi$

$exp_g ::=$	$z \mid null \mid f(exp_g, \ldots, exp_g) \mid exp_g.x$	$E \in GExp$
$ass_g ::=$	$exp_g \mid \neg ass_g \mid ass_g \land ass_g \mid \exists z. \ ass_g$	$P \in GAss$

Table 3. Syntax of assertions

restricted quantifications  $\exists z \in e.p$  or  $\exists z \sqsubseteq e.p$ . The local assertion  $\exists z \in e.p$  states that there is a value z in the sequence e, for which p holds;  $\exists z \sqsubseteq e.p$  states the existence of a subsequence. Global assertions are evaluated in the context of a global state. Thus, unrestricted quantification is allowed for all types and ranges over the set of *existing* values. Qualified references E.x may be used in the global language only. We write  $[\![-]\!]_{\mathcal{L}}$  and  $[\![-]\!]_{\mathcal{G}}$  for the semantic functions evaluating local and global assertions, and  $\omega, \sigma_{inst}, \tau \models_{\mathcal{L}} p$  for  $[\![p]\!]_{\mathcal{L}}^{\omega,\sigma_{inst},\tau} = true$ , and  $\models_{\mathcal{L}} p$  if pholds in all contexts; we use analogously  $\models_{\mathcal{G}}$  for global assertions.

To express a local property p in the global assertion language, we define the lifting substitution p[z/this] by simultaneously replacing in p all occurrences of this by z, and transforming all occurrences of instance variables x into qualified references z.x, where z is assumed not to occur in p. For notational convenience we view the local variables occurring in the global assertion p[z/this] as logical variables. Formally, these local variables are replaced by fresh logical variables. We will write P(z) for p[z/this], and similarly for expressions.

For technical convenience, in this paper we formulate verification conditions as standard Hoare-triples  $\{\varphi\}$  stm  $\{\psi\}$ . The statements of these Hoare-triples may also contain assignments involving qualified references as given by the global assertion language. The formal semantics is given by means of a weakest precondition calculus [8, 4].

# 4 The proof system

The following section defines how to augment and annotate programs resulting in proof outlines, before Section 4.2 describes the proof method. The proof system accommodates for dynamic object creation, shared-variable concurrency, aliasing, method invocation, synchronization, and, especially, the reentrant monitors. Missing details can be found in [4].

### 4.1 **Proof outlines**

The definition of a relatively complete proof system requires that we can encode the transition semantics of  $Java_{MT}$  in the assertion language. As the assertion language can reason about the local and global states, only, we have to *augment* programs with fresh auxiliary variables to represent information about

## The proof system

#### Fig. 1. Augmentation and annotation: Synchronized method call, start

the control points and stack structures within the local and global states: Assignments y := e can be extended to multiple assignments  $y, \vec{y}_{aux} := e, \vec{e}_{aux}$  by inserting additional assignments to distinct auxiliary variables  $\vec{y}_{aux}$ . Additional auxiliary assignments can be inserted at any control point. Observations  $\vec{y} := \vec{e}$ of communication and object creation stm are enclosed in *bracketed sections*  $\langle stm; \vec{y} := \vec{e} \rangle$ . Method calls and the reception of the return value is observed by  $\langle e_0.m(\vec{e}); \vec{y}_1 := \vec{e}_1 \rangle$  and  $\langle \text{receive } u_{ret}; \vec{y}_4 := \vec{e}_4 \rangle$ . Similarly for the callee, methods are extended to  $m(\vec{u})\{\langle \vec{y}_2 := \vec{e}_2 \rangle; stm; \langle \text{return } u_{ret}; \vec{y}_3 := \vec{e}_3 \rangle\}$ . To be uniform, we will sometimes write  $\langle ?m(\vec{u}); \vec{y} := \vec{e} \rangle$  to indicate that the assignment observes the reception of a method call. We require that the caller observation in a self-communication does not change the values of instance variables.

Bracketed sections do not influence the control flow of the original program but enforce a particular scheduling policy: Communication, sender, and receiver observations are executed in this order in a single computation step, i.e., they cannot be interleaved with other threads. Points which can be interleaved we call control points. At points between communication and its observation in bracketed sections, or at the beginning and at the end of a methods, no interleaving can take place; we call them *auxiliary points*.

Next we introduce a few auxiliary variables, built into all augmentations and used in the verification conditions. Their values are changed only as described in the following. The updating of the specific auxiliary variables for ordinary synchronized methods and for the start-method is illustrated in Figure 1. Nonsynchronized methods are treated analogously except that they do not change the lock value; the start-method additionally handles thread creation.

Figure 2 shows the augmentation of the monitor methods. Note that we do not use the auxiliary statements !signal, !signal\_all, and ?signal in the proof outlines and implement the monitore methods with the auxiliary variables wait and notified, instead, which represent the corresponding sets of the semantics.

An important point of the proof system is the identification of communicating objects and threads. We identify a thread by the object in which it has begun its execution. The identification is unique as an object's thread can be started only once. This identity is handed over from caller to callee as auxiliary formal parameter thread. For the start-method we use caller\_thread as additional formal

Fig. 2. Augmentation and annotation: Signaling

parameter to store the identity of the caller thread. A local configuration, which represents the execution of a method, is identified by the object in which it executes together with the value of its auxiliary local variable **conf** storing a unique object-internal identifier. Its uniqueness is assured by the auxiliary instance variable **counter**, incremented for each new local configuration in that object. The callee receives the "return address" as auxiliary formal parameter **caller**, given by the caller object together with the identity of the calling local configuration. The **main**-method is initially executed with the parameters  $((nil, 0), \alpha_0)$ , where  $\alpha_0$  is the initial object.

To capture mutual exclusion and the monitor discipline, the instance variable lock of type  $Object \times Int + free$ , with initial value *free*, stores the identity of the thread that owns the lock, if any, together with the number of reentrant synchronized calls in the call chain. The semantics of incrementing the lock  $\llbracket \operatorname{inc}(\operatorname{lock}) \rrbracket_{\mathcal{E}}^{\sigma_{inst},\tau}$  is  $(\tau(\operatorname{thread}), 0)$  for  $\sigma_{inst}(\operatorname{lock}) = free$ , and  $(\alpha, n+1)$  for  $\sigma_{inst}(\mathsf{lock}) = (\alpha, n)$ . Decrementing  $\mathsf{dec}(\mathsf{lock})$  is done inversely. The instance variables wait and notified of type  $2^{\mathsf{Object} \times \mathsf{Int}}$ , with initial value  $\emptyset$ , are the analogues of the *wait*- and *notified*-sets of the semantics and store the threads waiting at the monitor, respectively, those having been notified. Besides the thread identity, the number of reentrant synchronized calls is stored. In other words, the wait and notified sets remember the old lock-value prior to suspension which is restored when the thread becomes active again. The old value is given by  $get(notified, \alpha)$  for a thread  $\alpha$ , whose uniqueness is assured by the semantics. The value notify(wait, notified) is the pair of the given sets with one element, chosen nondeterministically, moved from the wait into the notified set; if the wait set is empty, it is the identity function. Note that in the augmented wait-method both the waiting and the notified status of the executing thread are represented by a single control point. The two statuses can be distinguished by the values of the wait and notified variables. The boolean instance variable started, finally, remembers whether the object's start-method has already been invoked. All aux-

8

## The proof system

iliary variables are initialized as usual, except the started-variable of the initial object which gets the value true.

To specify invariant properties of the system, the augmented programs are annotated by attaching local assertions to each control and auxiliary point. We use the standard triple notation  $\{p\}$  stm  $\{q\}$  and write pre(stm) and post(stm)to refer to the pre- and the post-condition of a statement. Besides that, for each class c, a local assertion  $I_c$  called *class invariant* specifies invariant properties of instances of c in terms of its instance variables. We require that the pre- and postconditions of whole method bodies, describing the instance state of the callee object directly before method call and after returning, respectively, are given by the class invariant.<sup>3</sup> Finally, the global invariant  $GI \in GAss$  specifies properties of communication between objects. As such, it should be invariant under objectinternal computation. For that reason, we require that for all qualified references E.x in GI with E of type c, all assignments to x in class c occur in bracketed sections of communication or object creation. Note that the global invariant is not affected by the object-internal monitor signaling mechanism. We require that in the annotation no free logical variables occur. An augmented and annotated program proq' is called a proof outline.

## 4.2 Verification conditions

The proof system formalizes a number of *verification conditions* which inductively ensure that for each *reachable* configuration the assertions at all current control points are satisfied, and that the global and the class invariants hold. The conditions are grouped, as usual, into initial conditions, local correctness, interference freedom, and a cooperation test. Note that the proof method is *modular* in that it allows for separate interference freedom and cooperation tests.

Arguing about two different local configurations makes it necessary to distinguish between their local variables, since these possibly have the same names; in such cases we rename the local variables in one of the local states. We use primed assertions p' to denote a given assertion p with every local variable ureplaced by a fresh one u', and do so, correspondingly, for expressions.

**4.2.1** Local correctness A proof outline is *locally correct*, if the properties of method instances as specified by the annotation are invariant under their own execution. For example, an assignment's precondition must imply its postcondition after execution. Besides that, invariance of the class invariant is required.

**Definition 1 (Local correctness: Assignment).** A proof outline is locally correct, if for all assignments  $\{p_1\} \vec{y} := \vec{e} \{p_2\}$  outside bracketed sections and all c,

$$\models_{\mathcal{L}} \{p_1\} \quad \vec{y} := \vec{e} \quad \{p_2\} \tag{1}$$

$$\models_{\mathcal{L}} p_1 \to I_c . \tag{2}$$

<sup>&</sup>lt;sup>3</sup> Note that the callee configuration directly *after* invocation is described by the postcondition of the callee observation  $\langle stm \rangle^{\circ_{call}}$ , which can be an arbitrary local assertion.

The conditions for loops and conditional statements are similar. Note that we have no local verification conditions for observations of communication and object creation. The postconditions of such statements express *assumptions* about the communicated values. They will be verified in the *cooperation test*.

**4.2.2** The interference freedom test Invariance of local assertions under computation steps in which they are not involved is assured by the *interference freedom test*. Since  $Java_{MT}$  does not support qualified references to instance variables, we only have to deal with invariance under execution within the *same* object. Affecting only local variables, communication and object creation do not change the instance states of the executing objects. Thus we only have to cover invariance of assertions annotating control points over assignments, including those of bracketed sections. Assertions at auxiliary points do not have to be shown invariant. So let p be an assertion at a control point and  $\vec{y} := \vec{e}$  an assignment in the same class. In the following we will prime local variables of the assertion to distinguish them from those of the assignment.

The assertion p has to be invariant under the assignment only if the assignment is executed independently of the control point annotated by p:

$$\begin{split} \mathsf{interferes}(p,\vec{y}:=\vec{e}) &\stackrel{aej}{=} \mathsf{thread} \neq \mathsf{thread}' \to \neg \mathsf{self\_start}(p,\vec{y}:=\vec{e}) \land \\ \mathsf{thread} = \mathsf{thread}' \to \mathsf{waits\_for\_ret}(p,\vec{y}:=\vec{e}) \,. \end{split}$$

1.0

The definition distinguishes two cases: If the assertion and the assignment belong to *different* threads, interference freedom must be shown in any case except for the self-invocation of the start-method. If they belong to the *same* thread, the only assertions endangered are those at control points waiting for a return value earlier in the thread's stack. Invariance of a local configuration under its own execution, however, need not be considered and is excluded by requiring conf  $\neq$  conf'. Interference with the *matching* return statement in a self-communication neither needs to be considered, because communicating receive and return statements are executed simultaneously. This particular case is excluded by additionally requiring caller  $\neq$  (this, conf') for such assertionassignment pairs.

**Definition 2 (Interference freedom).** A proof outline is interference free, if for all classes c, assignments  $\{p\}\vec{y} := \vec{e}$ , and assertions q at control points in c,

$$\models_{\mathcal{L}} \{ p \land q' \land \mathsf{interferes}(q, \vec{y} := \vec{e}) \} \quad \vec{y} := \vec{e} \quad \{q'\} . \tag{3}$$

**4.2.3** The cooperation test Whereas the interference freedom test assures invariance of assertions under steps in which they are not involved, the *cooperation test* deals with inductivity for communicating partners, assuring that the global invariant and the preconditions of the involved bracketed sections imply their postconditions after the joint step. Additionally, the assertions at the auxiliary points must hold immediately after communication. The global invariant

may refer only to auxiliary instance variables which are changed in bracketed sections. Consequently, it is automatically invariant under the execution of noncommunicating statements. For bracketed sections of communication and object creation, however, the invariance must be shown as part of the cooperation test.

In the following we define the cooperation test for method call. Since different objects may be involved, the cooperation test is formulated in the global assertion language. Local properties are expressed in the global language using the lifting substitution. To avoid name clashes between local variables of the partners, we rename those of the callee by priming them.

Let z and z' be logical variables representing the caller, respectively, the callee object. We assume the global invariant and the preconditions of the communicating statements to hold prior to communication. For method invocation, the precondition of the callee is its class invariant, as defined in the annotation. That the assertions indeed represent communicating partners and that the communication is enabled is captured in the assertion **comm**: In case of a synchronized method invocation, the lock of the callee object has to be free or owned by the caller, which is expressed by  $z'.lock = free \lor thread(z'.lock) = thread$ , where thread is the caller thread and  $thread(\alpha, n) = \alpha$ . For the invocation of the monitor methods the executing thread must hold the lock.

Let the function  $Init: Var \rightarrow Val_{nil}$  assign to each variable its initial value.

**Definition 3 (Cooperation test: Method invocation).** A proof outline satisfies the cooperation test for method invocation, if for all statements of the form  $\{p_1\}\langle e_0.m(\vec{e}); \{p_2\}\vec{y_1} := \vec{e_1}\rangle\{p_3\}$  in class c with  $e_0$  of type c', where method m of c' has body  $\{q_1\}\langle m(\vec{u}); \{q_2\}\vec{y_2} := \vec{e_2}\rangle; \{q_3\}$ stm and local variables  $\vec{v}$  except the formal parameters:

$$\begin{split} \models_{\mathcal{G}} & \{GI \land P_{1}(z) \land Q'_{1}(z') \land \mathsf{comm} \} \\ & \vec{u}', \vec{v}' := \vec{E}(z), \mathsf{lnit}(\vec{v}) \\ & \{P_{2}(z) \land Q'_{2}(z') \} \\ \models_{\mathcal{G}} & \{GI \land P_{1}(z) \land Q'_{1}(z') \land \mathsf{comm} \} \\ & \vec{u}', \vec{v}' := \vec{E}(z), \mathsf{lnit}(\vec{v}); \quad z.\vec{y}_{1} := \vec{E}_{1}(z); \quad z'.\vec{y}'_{2} := \vec{E}'_{2}(z') \\ & \{GI \land P_{3}(z) \land Q'_{3}(z') \}, \end{split}$$

where  $z \in LVar^c$  and  $z' \in LVar^{c'}$  are distinct and fresh; comm is given by  $E_0(z) = z' \wedge z \neq \text{nil} \wedge z' \neq \text{nil} \wedge \text{synch}$ , and with synch defined as

- true for  $m \notin \{\text{start}, \text{wait}, \text{notify}, \text{notifyAll}\}\ non-synchronized,$
- $z'.lock = free \lor thread(z'.lock) = thread for m \notin {start, wait, notify, notifyAll} synchronized,$
- thread(z'.lock) = thread for  $m \in \{$ wait, notify, notifyAll $\}$ , and
- $-\neg z'$ .started for m = start.

For m = start, the conditions must hold with additionally synch as z'.started, where  $q_2 = q_3 = \text{true}$  and without  $\vec{u}', \vec{v}' := \vec{E}(z), \text{Init}(\vec{v})$  and  $z'.\vec{y}'_2 := \vec{E}'_2(z')$ .

```
...{owns(thread, lock)}
 1
       (this.wait(this,conf,thread));
 2
                 \{\neg owns(thread, lock) \land (this, conf) = getcaller(x, thread)\}
 3
 4
       (receive)
                 \{owns(thread, lock)\}\dots
 \mathbf{5}
       {true} nsync wait (caller,thread) {
 7
                  {owns(thread, lock)}
 8
           \begin{array}{l} \langle \texttt{conf:=counter, counter:=counter + 1, lock:=free,} \\ \texttt{wait:=wait} \ \cup \ \{\texttt{lock}\}, \ \texttt{x:=x} \ \circ \ (\texttt{thread,caller}) \rangle; \\ \{ \neg \textit{owns}(\textit{thread, lock}) \land \textit{caller} = \textit{getcaller}(x, \textit{thread}) \} \end{array} 
 9
10
11
12
           (return getlock;
                 \{lock = free \land caller = getcaller(x, thread) \land thread \in notified\}
13
            lock:=get(notified,thread)
14
            notified:=notified \setminus get(notified,thread)\rangle } {true}
15
```

#### Fig. 3. Example

The first verification condition justifies the assertions at the auxiliary points after parameter passing, whereas the second verification condition justifies the postconditions of the bracketed sections and invariance of the global invariant.

For returning from a method and for object creation, there are similar conditions. Here we remark only that returning from the wait-method assumes that the thread has been notified and that the lock of the given object is free; in this case, synch is defined by z'.lock = free  $\land$  thread'  $\in z'$ .notified (with  $\alpha \in notified$ iff there is a  $(\alpha, n) \in notified$  for some n).

The verification conditions presented above give rise to a *sound* and *relative complete* proof system. This means if all the verification conditions are valid, then at each reachable point all assertions hold, and conversely, if a program satisfies the requirements asserted in its proof outline, then this is indeed provable, i.e., then there exists a proof outline which can be shown to hold and which implies the given one. For the exact (standard) formulation of soundness and completeness and their proofs, we refer to the technical report [4].

**4.2.4** Example We conclude this section with an example shown in Figure 3 which presents an annotation of the wait-method and its self-invocation. The annotation expresses basic properties of the lock ownership. The history of all invocations of the wait method is recorded in the auxiliary instance variable x of type list(Object × (Object × lnt)). The operation getcaller(x, thread) returns caller where (thread, caller) is the last element in x with first component thread. We use owns(thread, lock) as shorthand for thread = thread(lock).

The proof uses the interference freedom test and the cooperation test; we start with the latter. The postconditions (3) and (9) of the method invocation at (2) and its observation at (8) is justified in the cooperation test as the postcondition of the parameter passing followed by the observation; note that (7) follows directly from (1) by parameter passing. Remember that we rename the

12

## Conclusion

local variables of the callee. The cooperation test for returning from the waitmethod, i.e., the simultaneous execution of (4) and (10), additionally imports the information described by the assertion synch, namely that the lock is free and the executing thread is already notified.

To show interference freedom, we proceed by case analysis. For interference between different threads, assume thread  $\neq$  thread'. For example, the assertion at (1) is invariant under the execution of (8) by a different thread, because the lock can be owned by at most one thread. Formally, the conjunction of (1) and (7) gives us owns(thread', lock)  $\land$  owns(thread, lock) contradicting our assumption thread  $\neq$  thread'. The other cases follow similarly from the assumption.

More interesting is interference with respect to one thread, where we only need to consider invariance of the primed assertion at (3) over the assignments at (8) and (12). For (8), it suffices to observe that the assertions (3) and (7) lead to a contradiction with the assumption thread = thread'. The most interesting case is the invariance of the assertion (3) under the execution of (12). The information about the auxiliary variable x and the assumption that we deal with a single thread implies caller = (this, conf'). This information contradicts the interleavable predicate of the interference freedom test, which excludes the situation of a matching return-receive statements in a self-communication.

## 5 Conclusion

This paper presents the first sound and complete assertional proof method for a multithreaded sublanguage of Java including its monitor discipline. It extends earlier work [5] by integrating Java's wait and notify constructs into the proof system and by moving towards a more compositional formulation of the identification mechanism for threads, corresponding to the compositional semantics in [3]. Moreover, this particular extension shows how to incorporate further control mechanism by means of auxiliary variables which describe the corresponding flow of control. Based on the proof theory presented here, we have developed a front-end tool Verger which automatically extends programs with the built-in augmentation and generates the verification conditions for the theorem prover PVS. In [4], we explore the tool on a few examples, and present an extension of the proof theory to show absence of deadlock.

Related work As far as proof systems and verification support for object-oriented programs is concerned, research has mostly concentrated on *sequential* languages. For instance, the LOOP-project [14, 17] develops methods and tools for the verification of sequential object-oriented languages, based on coalgebras and using proof PVS and Isabelle/HOL. Poetzsch-Heffter and Müller [20] develop a Hoare-style programming logic presented in sequent formulation for a sequential kernel of Java, featuring interfaces, subtyping, and inheritance. Translating the operational and the axiomatic semantics into the HOL theorem prover allows a computer assisted soundness proof. The work [21] uses a modification of the object constraint language OCL as assertional language to annotate UML class diagrams and to generate proof conditions for Java-programs. In [23] a large subset of JavaCard, including exception handling, is formalized in Isabelle/HOL, and its soundness and completeness is shown within the theorem prover. [18] presents an exectuable formalization of a simplified JVM within the theorem prover ACL2. The work in [2] presents a Hoare-style proof-system for a sequential object-oriented calculus [1]. The language features heap-allocated objects (but no classes), side-effects and aliasing, and its type system supports subtyping. Furthermore, the language allows nested statically let-bound variables, which requires a more complex semantical treatment for variables based on closures, and ultimately renders their proof-system incomplete. Its assertion language is presented as an extension of the object calculus' language of type and analogously, the proof system extends the type derivation system. The close connection of types and specifications in the presentation is exploited in [22] for the generation of verification conditions. A survey about monitors in general, including proof-rules for various monitor semantics, can be found in [7].

The extended static checking approach [9,15] occupies a middle-ground between verification and static analysis. Based on an intermediate guarded command language, the ESC-tool statically tries to detect (amongst other static properties) programming errors typical in a multithreaded setting such as synchronization errors and race conditions. In this direction, [10] presents a threadmodular checking approach based on assume-guarantee reasoning and implemented in the *Calvin*-tool.

Future work We plan to extend  $Java_{MT}$  by further constructs, like exceptions, inheritance, and subtyping. To deal with subtyping on the logical level requires a notion of behavioral subtyping.

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