
Verification for Java's Monitor Concept

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- Programming language $Java_{MT}$
- Assertion language
- Proof system
- Conclusion

- safety-critical application areas
→ need for verification
- model checking: mostly for finite state systems
- existing deductive methods: mostly for sequential *Java*

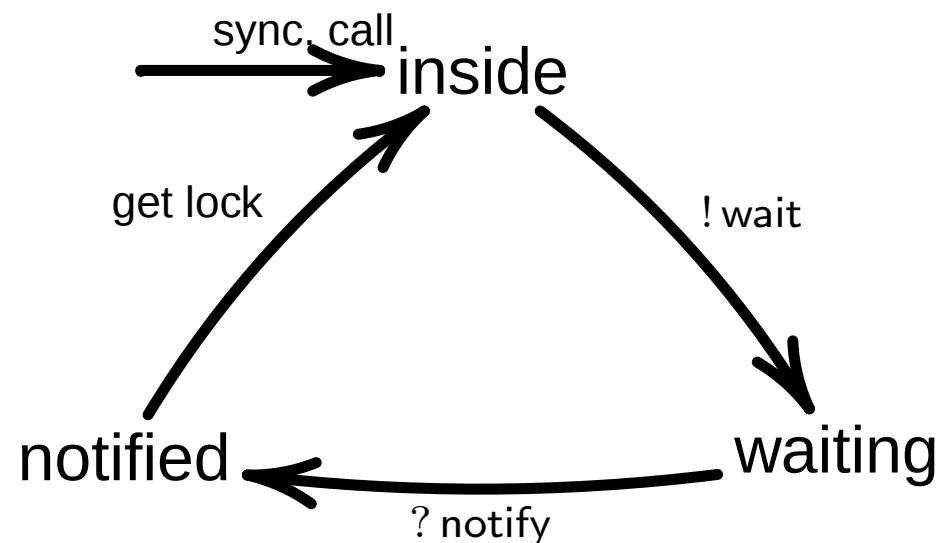
Multithreading core of Java

Object of study: *Java_{MT}*

- heap-allocated objects, aliasing
- object creation
- method invocation, recursion, self-calls
- **multithreading**
- **wait & notify monitor** synchronization
- not covered (yet): inheritance, polymorphism, exceptions ...

- **threads** = sequential sequence of actions
- method calls/returns: **stack** of method bodies, each with **local** variables
- running in **parallel**
- **sharing** instance states
- **dynamically created** as instances of thread classes (+ explicitly **started**)

- each object can act as **monitor**:
 - **mutual exclusion** between *synchronized* methods of a single instance
 - monitor **coordination** via methods: **wait**, **notify**, **notifyAll**



Abstract syntax

$$\begin{aligned} \text{exp} &::= x \mid u \mid \text{this} \mid \text{nil} \mid f(\text{exp}, \dots, \text{exp}) \\ \text{stm} &::= x := \text{exp} \mid u := \text{exp} \mid u := \text{new}^c \\ &\quad \mid \text{exp}.m(\text{exp}, \dots, \text{exp}); \text{receive } u \mid \text{exp}.start() \\ &\quad \mid \epsilon \mid \text{stm}; \text{stm} \mid \text{if } \text{exp} \text{ then } \text{stm} \text{ else } \text{stm} \text{ fi } \dots \\ \text{modif} &::= \text{nsync} \mid \text{sync} \\ \text{meth} &::= \text{modif } m(u, \dots, u) \{ \text{stm}; \text{return } \text{exp} \} \\ \text{meth}_{\text{predef}} &::= \text{meth}_{\text{run}} \text{ meth}_{\text{start}} \text{ meth}_{\text{wait}} \text{ meth}_{\text{notify}} \text{ meth}_{\text{notifyAll}} \\ \text{class} &::= c \{ \text{meth} \dots \text{meth } \text{meth}_{\text{predef}} \} \\ \text{prog} &::= \langle \text{class} \dots \text{class } \text{class}_{\text{main}} \rangle \end{aligned}$$

- straightforward structural operational semantics
- transitions between global configurations

states

local	τ	values of local variables
global	σ	values of instance variables for each <i>existing</i> object

configurations

local	(τ, stm)	local state + point of exec.
thread	$(\tau_0, stm_0) \dots (\tau_n, stm_n)$	stack of local configurations
global	$\langle T, \sigma \rangle$	set of thread configurations + global state

Impressionistic view on SOS

$$\frac{\beta = \llbracket e \rrbracket_{\mathcal{E}}^{\sigma(\alpha), \tau} \in \text{dom}^c(\sigma) \quad \neg \text{started}(T \cup \{\xi \circ (\alpha, \tau, e.\text{start}()); \text{stm}\}), \beta)}{\langle T \dot{\cup} \{\xi \circ (\alpha, \tau, e.\text{start}()); \text{stm}\}, \sigma \rangle \longrightarrow \langle T \dot{\cup} \{\xi \circ (\alpha, \tau, \text{stm}), (\beta, \tau_{\text{init}}^{\text{start}, c}, \text{body}_{\text{start}, c})\}, \sigma \rangle} \text{CALL}_{\text{start}}$$

$$\frac{\beta = \llbracket e \rrbracket_{\mathcal{E}}^{\sigma(\alpha), \tau} \in \text{dom}^c(\sigma) \quad \text{started}(T \cup \{\xi \circ (\alpha, \tau, e.\text{start}()); \text{stm}\}), \beta)}{\langle T \dot{\cup} \{\xi \circ (\alpha, \tau, e.\text{start}()); \text{stm}\}, \sigma \rangle \longrightarrow \langle T \dot{\cup} \{\xi \circ (\alpha, \tau, \text{stm})\}, \sigma \rangle} \text{CALL}_{\text{start}}^{\text{skip}}$$

$$\frac{}{\langle T \dot{\cup} \{(\alpha, \tau, \text{return})\}, \sigma \rangle \longrightarrow \langle T \dot{\cup} \{(\alpha, \tau, \epsilon)\}, \sigma \rangle} \text{RETURN}_{\text{start}}$$

$$m \in \{\text{wait}, \text{notify}, \text{notifyAll}\}$$

$$\frac{\beta = \llbracket e \rrbracket_{\mathcal{E}}^{\sigma(\alpha), \tau} \in \text{dom}^c(\sigma) \quad \text{owns}(\xi \circ (\alpha, \tau, e.m()); \text{stm}), \beta)}{\langle T \dot{\cup} \{\xi \circ (\alpha, \tau, e.m()); \text{stm}\}, \sigma \rangle \longrightarrow \langle T \dot{\cup} \{\xi \circ (\alpha, \tau, \text{stm}) \circ (\beta, \tau_{\text{init}}^{m, c}, \text{body}_{m, c})\}, \sigma \rangle} \text{CALL}_{\text{monitor}}$$

$$\frac{\neg \text{owns}(T, \beta)}{\langle T \dot{\cup} \{\xi \circ (\alpha, \tau, \text{receive}; \text{stm}) \circ (\beta, \tau', \text{return}_{\text{getlock}})\}, \sigma \rangle \longrightarrow \langle T \dot{\cup} \{\xi \circ (\alpha, \tau, \text{stm})\}, \sigma \rangle} \text{RETURN}_{\text{wait}}$$

$$\frac{}{\langle T \dot{\cup} \{\xi \circ (\alpha, \tau, \text{!signal}; \text{stm})\} \dot{\cup} \{\xi' \circ (\alpha, \tau', \text{?signal}; \text{stm}')\}, \sigma \rangle \longrightarrow \langle T \dot{\cup} \{\xi \circ (\alpha, \tau, \text{stm})\} \dot{\cup} \{\xi' \circ (\alpha, \tau', \text{stm}')\}, \sigma \rangle} \text{SIGNAL}$$

$$\frac{\text{wait}(T, \alpha) = \emptyset}{\langle T \dot{\cup} \{\xi \circ (\alpha, \tau, \text{!signal}; \text{stm})\}, \sigma \rangle \longrightarrow \langle T \dot{\cup} \{\xi \circ (\alpha, \tau, \text{stm})\}, \sigma \rangle} \text{SIGNAL}_{\text{skip}}$$

$$\frac{T' = \text{signal}(T, \beta)}{\langle T \dot{\cup} \{\xi \circ (\alpha, \tau, \text{!signal_all}; \text{stm})\}, \sigma \rangle \longrightarrow \langle T' \dot{\cup} \{\xi \circ (\alpha, \tau, \text{stm})\}, \sigma \rangle} \text{SIGNAL}_{\text{ALL}}$$

Semantics, e.g., instantiation

- instantiating a new object:

$u := \text{new}^c$

- create a fresh object id (i.e., $\beta \notin \text{dom}(\sigma)$)
- initialize the instance state
- extend the heap
- store the new identity

$$\frac{\beta \text{ fresh} \quad \sigma_{inst} = \sigma_{inst}^{c, init} [\text{this} \mapsto \beta] \quad \sigma' = \sigma [\beta \mapsto \sigma_{inst}]}{\langle T \dot{\cup} \underbrace{\{\xi \circ (\alpha, \tau, u := \text{new}^c; stm)\}}_{\text{one thread}}, \sigma \rangle \longrightarrow \langle T \dot{\cup} \{\xi \circ (\alpha, \tau[u \mapsto \beta], stm)\}, \sigma' \rangle} \text{NEW}$$

Proof-theoretical challenges

- dynamic **object creation**
- **concurrency**, multithreading
 - shared variables concurrency within objects
 - communication via method calls, self-calls
 - monitor synchronization

The assertional proof system

- **proof outline**
 - augmentation by **auxiliary variables**/bracketed sections
 - **assertions**:
 - local **assertions** to all control points
 - **class invariant** for each class
 - **global invariant**
- **verification conditions** for
 - **initial** correctness
 - inductive step:
 - **local** correctness
 - **interference freedom** test
 - **cooperation** test

The assertion language

local sublanguage: properties of method execution

$$\begin{aligned} exp_l &::= z \mid x \mid u \mid \text{this} \mid \text{nil} \mid f(exp_l, \dots, exp_l) \\ ass_l &::= exp_l \mid \neg ass_l \mid ass_l \wedge ass_l \\ &\quad \mid \exists z:\text{Int}. ass_l \dots \\ &\quad \mid \exists(z:\text{Object}) \in exp_l. ass_l \mid \exists(z:\text{Object}) \sqsubseteq exp_l. ass_l \end{aligned}$$

global sublanguage: properties of communication

$$\begin{aligned} exp_g &::= z \mid exp_g.x \mid \text{nil} \mid f(exp_g, \dots, exp_g) \\ ass_g &::= exp_g \mid \neg ass_g \mid ass_g \wedge ass_g \mid \exists z. ass_g \end{aligned}$$

Interference freedom

- variables **shared** within one instance $\Rightarrow$ **interference**
- **when** exactly can different “executions” interfere?
 - **different** threads, except matching signalling communication pairs
 - **reentrant** code pieces of the **same** thread, except *matching* return-communication

$$\models_{\mathcal{L}} \quad pre(\vec{y} := \vec{e}) \wedge q' \wedge \text{interleavable}(q', \vec{y} := \vec{e}) \rightarrow q'[\vec{e}/\vec{y}]$$

where $\text{interleavable}(p, \vec{y} := \vec{e})$ is defined as

$$\begin{aligned} & (\text{thread} = \text{thread}' \rightarrow \text{waits_for_ret}(p, \vec{y} := \vec{e})) \wedge \\ & (\text{thread} \neq \text{thread}' \rightarrow \neg \text{gets_signalled}(p, \vec{y} := \vec{e})) . \end{aligned}$$

Coop. test for communication (call)

... $\{p_1\}$ $\langle e0.m(\text{this}, \text{conf}, \text{thread}, e); \{p_2\} \vec{y}_1 := \vec{e}_1 \rangle; \{p_3\}$
 $\langle \text{receive } u_{ret}; \{p_4\} \vec{y}_4 := \vec{e}_4 \rangle; \{p_5\} \dots$

$\{I_c\}$ sync m (caller, caller_thread, u) { $\{q_2\}$
 $\langle \text{conf} := \text{counter}, \text{counter} := \text{counter} + 1,$
 thread := caller_thread,
 lock := inc(lock), $\vec{y}_2 := \vec{e}_2 \rangle; \{q_3\}$
 ... $\{q_4\}$
 $\langle \text{return } e_{ret}; \{q_5\} \text{ lock} := \text{dec(lock)}, \vec{y}_3 := \vec{e}_3 \rangle \} \{I_c\}$

Coop. test for communication (call)

$$\begin{aligned} \models_{\mathcal{G}} \quad & GI \wedge P_1(z) \wedge Q'_1(z') \wedge \\ & \text{communicating} \wedge z \neq \text{nil} \wedge z' \neq \text{nil} \rightarrow \\ & (P_2(z) \wedge Q'_2(z')) \circ f_{comm} \wedge \\ & (GI \wedge P_3(z) \wedge Q'_3(z')) \circ f_{obs2} \circ f_{obs1} \circ f_{comm} \end{aligned}$$

- z, z' : distinct fresh logical variables
- $\text{communicating} =$

$$(E_0(z) = z') \wedge (z'.\text{lock} = \text{free} \vee \text{thread}(z'.\text{lock}) = \text{thread})$$

- $f_{comm} = [\vec{E}(z), \text{Init}(\vec{v})/\vec{u}', \vec{v}'], f_{obs1} = [\vec{E}_1(z)/z.\vec{y}_1],$
 $f_{obs2} = [\vec{E}'_2(z')/z'.\vec{y}_2].$

Coop. test for communication

- other kinds of communications: variations of the **communicating**-assertion (and the “observations”):
 - **return**: must match caller and callee
 - **monitor**-callers must own the lock
 - **start** can be called (effectively) only once
 - return from a **wait**-method must re-acquire the lock
 - return from a **start**-method . . .

Coop. test for object creation

$$\{p_1\} \langle u := \text{new}^c; \{p_2\} \vec{y} := \vec{e} \rangle \{p_3\}$$

- new object's id must be fresh
- heap extended $\Rightarrow$ range of (unbounded) quantification changes

$$\models_{\mathcal{G}} z \neq \text{nil} \wedge$$

$$\exists z' : \text{list Object.} \left(\text{Fresh}(z', u) \wedge (GI \wedge \exists u. P_1(z)) \downarrow z' \right) \rightarrow \\ P_2(z) \wedge I_c(u) \wedge (GI \wedge P_3(z)) \circ f_{obs} ,$$

- $\text{Fresh}(z', u) = \text{InitState}(u) \wedge u \notin z' \wedge \forall v. v \in z' \vee v = u$

Coop. test for notification

```
{Ic} nsync wait (caller, caller_thread) { {q2}  
  <conf := counter, counter := counter + 1, thread := caller_thread,  
    wait := wait ∪ {lock}, lock := free,  $\vec{y}_2' := \vec{e}_2'$ >;  
  {q3} <?signal; {q4}  $\vec{y}' := \vec{e}'$ ; {q5}  
  <returngetlock; {q6} lock := get(notified, thread),  
    notified := notified get(notified, thread),  $\vec{y}_3' := \vec{e}_3'$ > {Ic}
```



```
{Ic} nsync notify (caller, caller_thread) { {p2}  
  <conf := counter, counter := counter + 1, thread := caller_thread;  $\vec{y}_2 := \vec{e}_2$ >;  
  {p3} <!signal {p4} notified := notified ∪ get(wait, partner),  
    wait := wait \ get(wait, partner),  $\vec{y} := \vec{e}$ >; {p5}  
  <return; {p6}  $\vec{y}_3 := \vec{e}_3$ > {Ic}
```

Coop. test for notification

$$\models_{\mathcal{L}} p_3 \wedge q'_3 \rightarrow (p_4 \wedge q'_4) \circ f_{comm} \wedge (p_5 \wedge q'_5) \circ f_{obs} \circ f_{comm} ,$$

where $f_{comm} = [\{\text{thread}'\}/\text{partner}]$,

- formulated in the **local** assertion language
- similar conditions for
 - **notifyAll** = **broadcast**
 - signalling **without** receiver

Auxiliary variables

- thread/object identification: aux. **formal parameters**
 - caller's **object id**
 - id of caller's **local configuration** = “return address”^a
 - id of **caller thread**
- capture monitor discipline: aux. **instance variables**
 - **lock** : $\text{Object} \times \text{Int} + \text{free}$
 - **wait, notified** : $2^{\text{Object} \times \text{Int}}$

⇒ The proof system is **sound** and (relative) **complete**

^aand mechanism for unique identifier of local configurations within an object, e.g., counter.

- de Boer, Amerika (Pool) [AdB93] ...
- Poetzsch-Heffter, Müller [PHM99], sequential *Java*.
- M. Huismann, B. Jacobs, et.al (Loop, PVS+Isabelle) [HHJT98] ...
- etc.

Future work:

- inheritance etc
- refined semantics: deadlocks-sensitive
- component-based extension
- compositionality
- PVS implementation under way

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